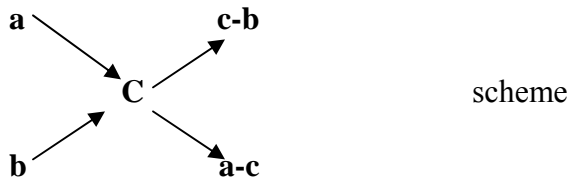


Account interference

First we will do a general task that will help us to solve other such tasks.

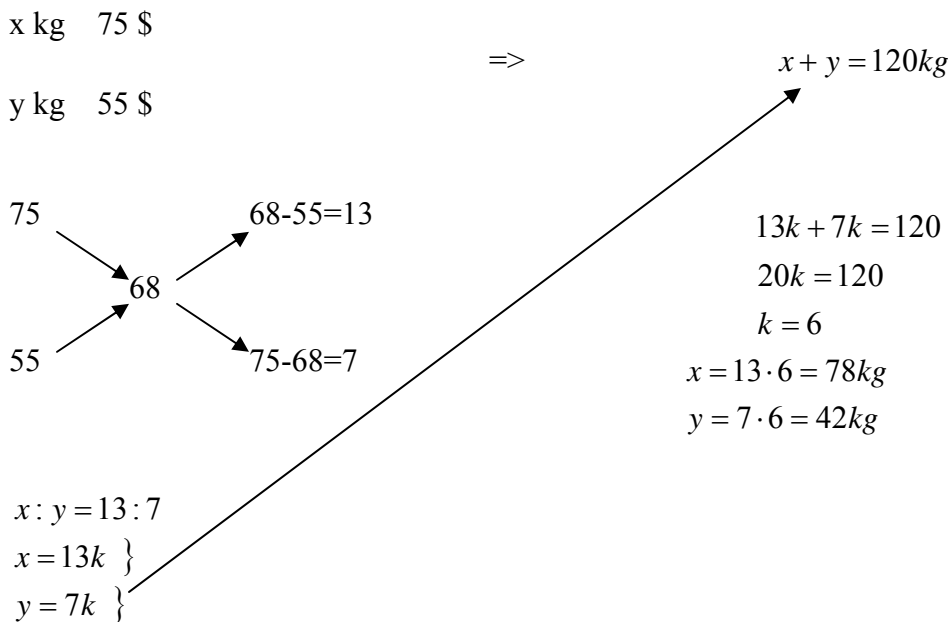
You must stir the two types of goods, whose prices are **a** \$ per kg and **b** \$ per kg, to received the goods at a price of **c** \$ per kg, ($b < c < a$). Determine the scale of this should interfere two types of goods.



If we take x kg of goods at the price of **a** \$, y kg at the cost of **b** \$, then:

$$x : y = (c - b) : (a - c)$$

1) On the stock has coffee at a price of 75 \$ per kg and 55 \$ per kg. Create a 120 kg mixture, which will sell at 68 \$ per kg.



Of course, this task can be solved with system:

$$\begin{array}{r}
 75 \cdot x + 55 \cdot y = 68 \cdot (x + y) \\
 x + y = 120 \text{ kg} \\
 \hline
 75x + 55y = 68 \cdot 120 \\
 x + y = 120 \\
 \hline
 75x + 55y = 8160 \\
 x + y = 120 \\
 \hline
 \end{array}$$

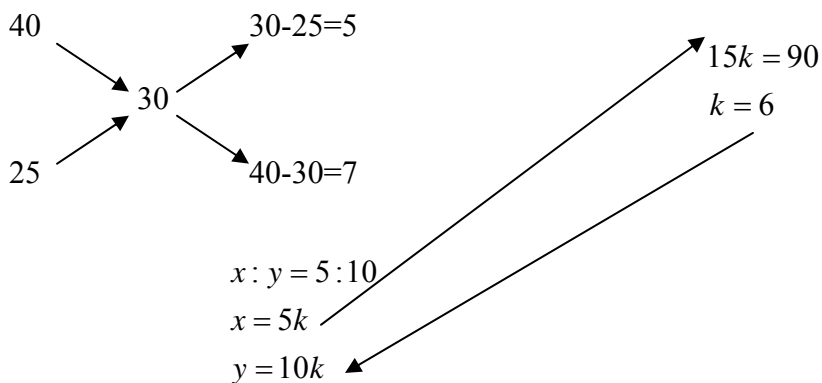
$$\begin{aligned}
 x &= 120 - y \rightarrow \text{Express one unknown and change it to another equation} \\
 75(120 - y) + 55y &= 8160 \\
 9000 - 75y + 55y &= 8160 \\
 -75y + 55y &= 8160 - 9000 \\
 -20y &= -840 \\
 y &= 42 \text{ kg}
 \end{aligned}$$

$$x = 120 - 42$$

$$x = 78 \text{ kg}$$

2) How much water temperature 40°C and water temperature 25°C should be mixed to obtain 90 liters of water temperature 30°C ?

$$\begin{array}{l}
 x \text{ liters } 40^\circ \text{C} \\
 y \text{ liters } 25^\circ \text{C}
 \end{array}
 \Rightarrow x + y = 90 \text{ l}$$



$$x = 30 \text{ l} \quad \text{and} \quad y = 60 \text{ l}$$

Over systems, would be:

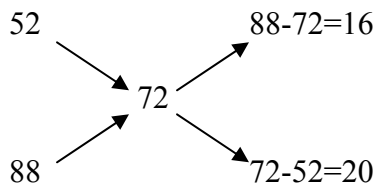
$$40 \cdot x + 25y = 90 \cdot 30$$

$$x + y = 90$$

3) How should be mixed acid strength 52% and 88% to get mixture of 144 liters with strength 72 % ?

$$x \text{ l strength } 52\%$$

$$y \text{ l strength } 88\%$$



$$x : y = 16 : 20$$

$$x = 16k$$

$$y = 20k$$

$$x + y = 144$$

$$16k + 20k = 144$$

$$36k = 144$$

$$k = 4$$

$$x = 16 \cdot 4 = 64l$$

$$y = 20 \cdot 4 = 80l$$

Watch out: When we mix goods with 3 or more different prices, chart does not help!

4) The company has 4 types of flour at the price of 72 \$, 48 \$, 60 \$ and 66 \$ per kilogram. How much should be taken of any kind that price is 50 \$ per kilogram?

x kg by 72 \$

y kg by 48 \$

z kg by 60 \$

t kg by 66 \$

$$72x + 48y + 60z + 66t = 50(x + y + z + t)$$

$$72x + 48y + 60z + 66t = 50x + 50y + 50z + 50t$$

$$22x - 2y + 10z + 16t = 0$$

You can create a large number of scale! $x : y : z : t = ?$ HOW?

Three unknown we take arbitrarily and fourth we calculate:

$y=24, z=1, t=1$ → arbitrarily chosen

$$22x - 48 + 10 + 16 = 0$$

$$22x = 22$$

$$x = 1$$

So: $x : y : z : t = 1 : 24 : 1 : 1$